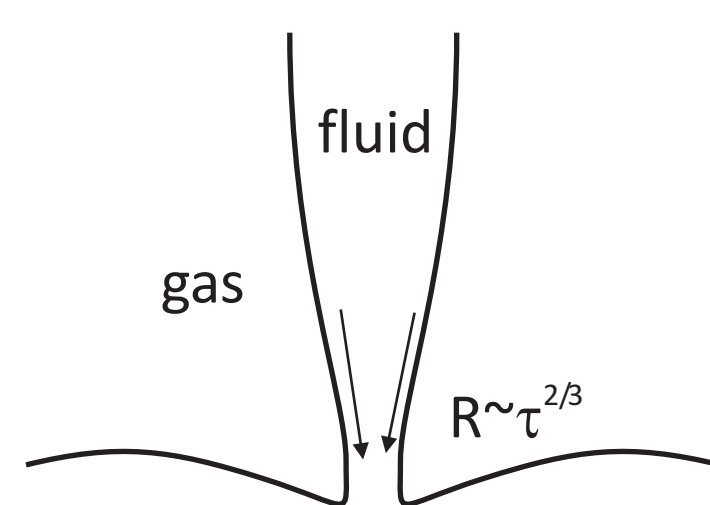


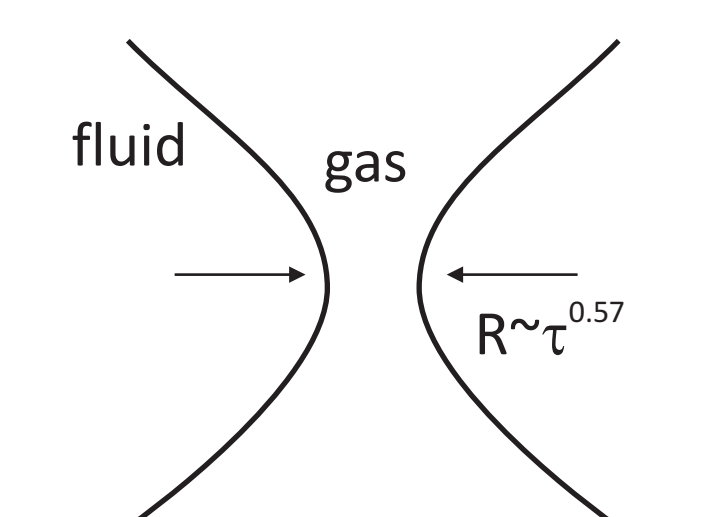
droplet pinch-off



The breakup and eventual pinch-off of inviscid droplet and bubble are two complementary problems with very different dynamics.

In fluid pinch-off the interface has an overturned profile and the minimum neck radius shrinks in a power-law fashion with an exponent of $2/3$, while the minimum neck radius of a bubble shrinks with an exponent ~ 0.57 , and asymptotically approaches $1/2$.

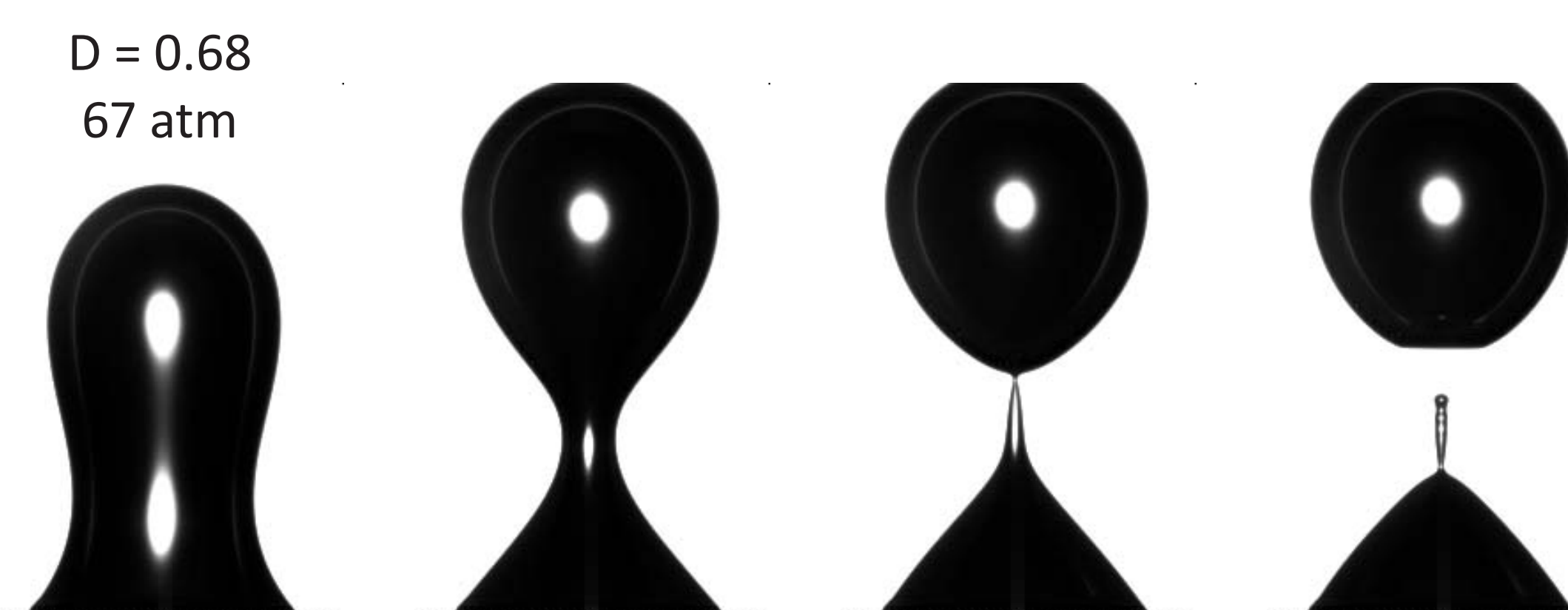
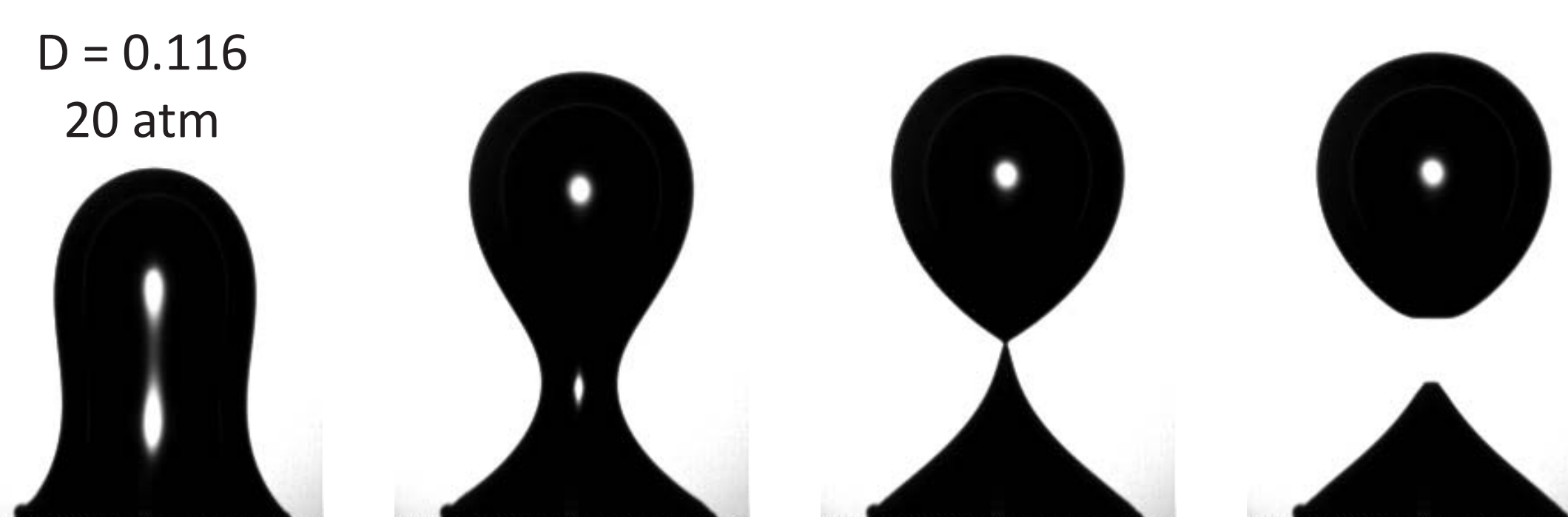
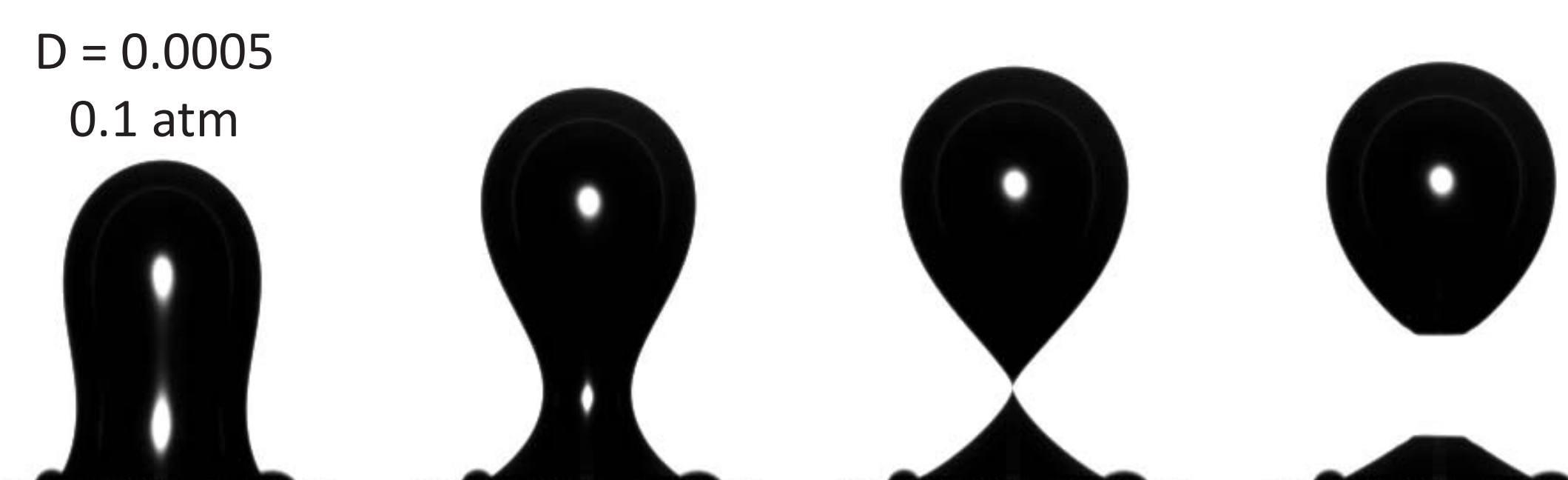
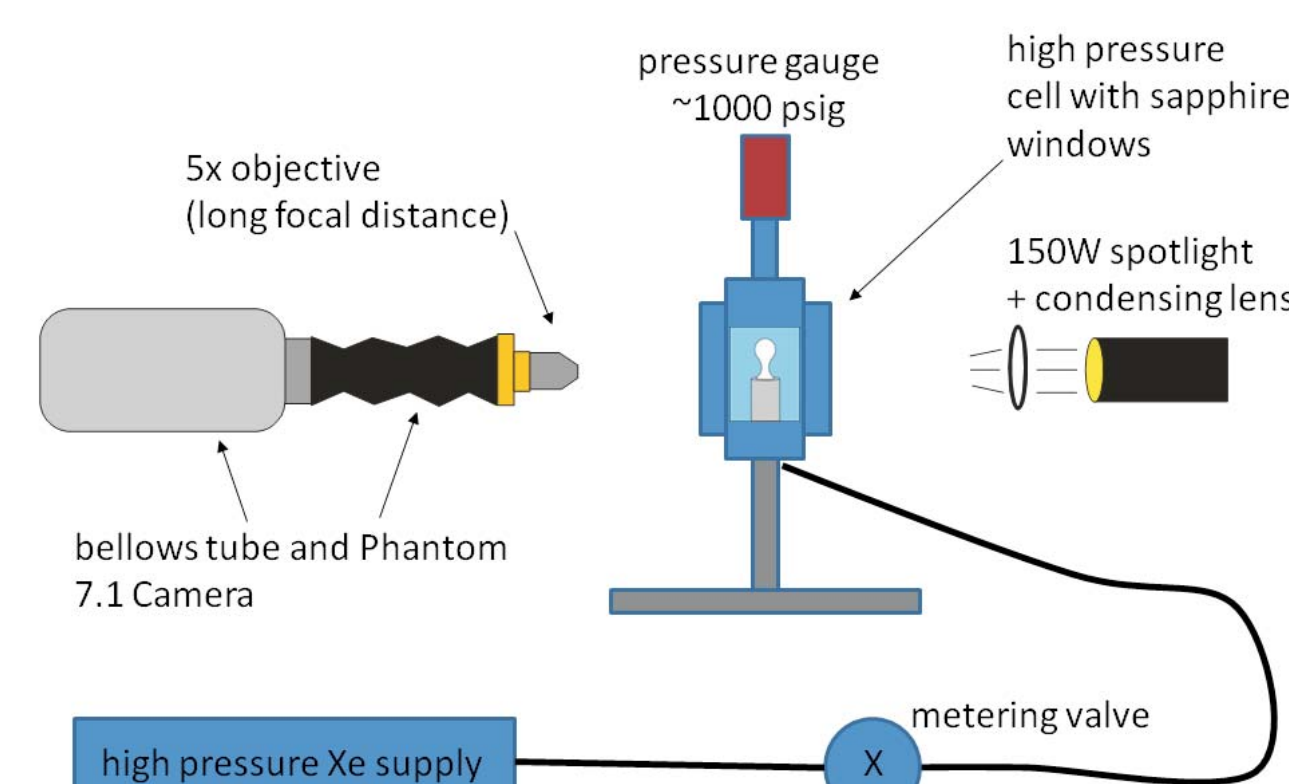
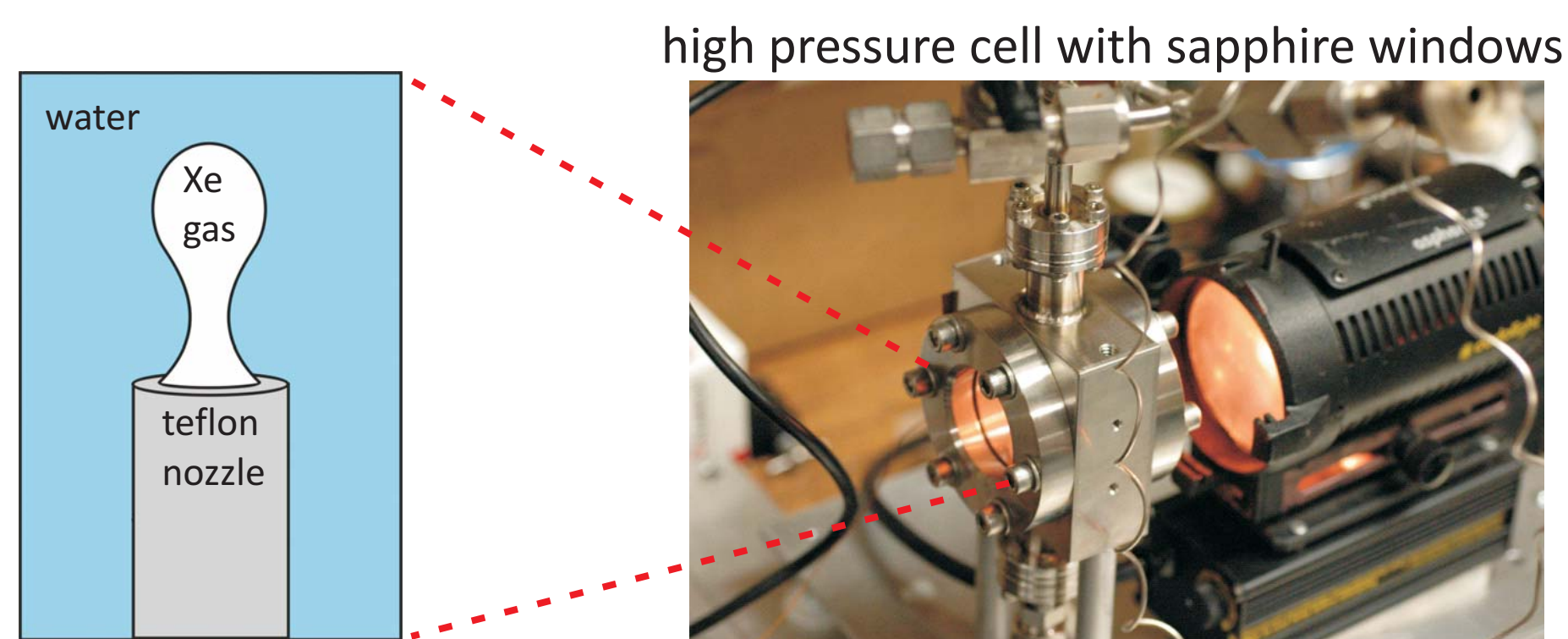
bubble pinch-off



Previously* we have explored the role of fluid viscosity in the pinch-off of air bubbles in water, our goal here is to explore the transition from bubble to droplet pinch-off using experiments and numerical simulations.

*J. C. Burton, R. Waldrep, and P. Taborek. Physical Review Letters 94, (184502).

Xenon Bubbles in Water - Density Effects



The purpose of this experiment is to explore the effects of density on the pinch-off of submerged bubbles.

Unlike a liquid, the density of a bubble can be changed dramatically simply by increasing the pressure.

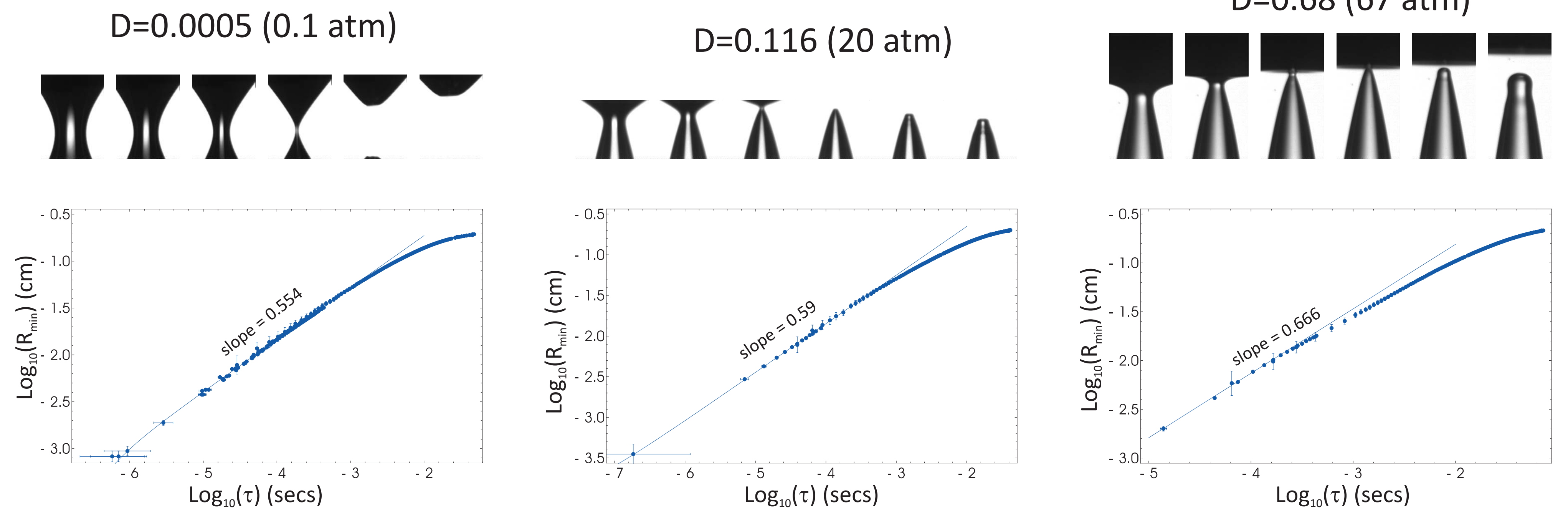
Gaseous xenon was used to change the density ratio D of the system from $D \approx 0$ to $D \approx 0.7$.

A specially designed high pressure cell (~ 100 atm) was constructed with sapphire windows in order to optically view the bubbles with a high-speed camera.

The three sequences on the left show the evolution of the xenon bubble at three density ratios. The diameter of the bubble is ~ 6 mm.

At high densities, the geometry of the pinching-region is similar to fluid pinch-off.

Time Dependence of Collapse



Measurements of the minimum neck radius (R_{min}) as a function of the time remaining until pinch-off (τ) for three different densities. The pictures are taken from the high-speed videos ($\sim 100,000$ frames per second) and are zoomed in on the pinch-off region. Our resolution is $\sim 2.4 \mu\text{m}/\text{pixel}$. In general, we see a smooth transition between bubble and droplet pinch-off, and at intermediate densities, the geometries and exponents that we observe fall in between that of bubble and droplet pinch-off.

Numerical Simulations of Bubble Pinch-off

The numerical simulations of pinch-off are performed using inviscid, boundary-integral techniques for initial shapes started from rest.

The density ratio between the interior and exterior fluid can be adjusted. On the immediate right, we see a bubble with a density ratio of $D=0.001$. As we increase the density ratio to $D=0.166$, we see an extremely unstable overturned interface. At higher density ratios ($D=0.68$), we see something qualitatively identical to that of droplet pinch-off.

The power-law exponents for each case is shown in the lower graphs. For $D=0.001$, we see that there is a transition in the exponent at short times, accompanied by the formation of a satellite bubble.

The data for $D=0.166$ is more difficult to interpret due to the complex structure, and the $D=0.68$ case produces a nearly perfect $2/3$ power-law.

